

Package ‘mvpd’

July 23, 2025

Title Multivariate Product Distributions for Elliptically Contoured Distributions

Version 0.0.5

Description Estimates multivariate subgaussian stable densities and probabilities as well as generates random variates using product distribution theory. A function for estimating the parameters from data to fit a distribution to data is also provided, using the method from Nolan (2013) <[doi:10.1007/s00180-013-0396-7](https://doi.org/10.1007/s00180-013-0396-7)>.

Imports matrixStats, stabledist, libstable4u, mvtnorm, stats, cubature, Matrix

Depends R (>= 3.4.0)

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Encoding UTF-8

RoxygenNote 7.2.1

Suggests scales, VGAMextra, expint, invgamma, LNPar, rgl, uniformly, rmarkdown, knitr, testthat (>= 3.0.0)

Config/testthat/edition 3

URL <https://github.com/swihart/mvpd>, <https://swihart.github.io/mvpd/>

BugReports <https://github.com/swihart/mvpd/issues>

NeedsCompilation no

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adaptIntegrate_inf_limPD

Adaptive multivariate integration over hypercubes (admitting infinite limits)

Description

The function performs adaptive multidimensional integration (cubature) of (possibly) vector-valued integrands over hypercubes. It is a wrapper for `cubature:::adaptIntegrate`, transforming (-)Inf appropriately as described in `cubature`'s help page (http://ab-initio.mit.edu/wiki/index.php/Cubature#Infinite_intervals).

Usage

```
adaptIntegrate_inf_limPD(
  f,
  lowerLimit,
  upperLimit,
  ...,
  tol.ai = 1e-05,
  fDim.ai = 1,
  maxEval.ai = 0,
  absError.ai = 0,
  doChecking.ai = FALSE
)
```

Arguments

<code>f</code>	The function (integrand) to be integrated
<code>lowerLimit</code>	The lower limit of integration, a vector for hypercubes
<code>upperLimit</code>	The upper limit of integration, a vector for hypercubes
<code>...</code>	All other arguments passed to the function <code>f</code>
<code>tol.ai</code>	The maximum tolerance, default 1e-5.

fDim.ai	The dimension of the integrand, default 1, bears no relation to the dimension of the hypercube
maxEval.ai	The maximum number of function evaluations needed, default 0 implying no limit
absError.ai	The maximum absolute error tolerated
doChecking.ai	A flag to be thorough checking inputs to C routines. A FALSE value results in approximately 9 percent speed gain in our experiments. Your mileage will of course vary. Default value is FALSE.

Examples

```
## integrate Cauchy Density from -Inf to Inf
adaptIntegrate_inf_limPD(function(x) 1/pi * 1/(1+x^2), -Inf, Inf)
adaptIntegrate_inf_limPD(function(x, scale) 1/(pi*scale) * 1/(1+(x/scale)^2), -Inf, Inf, scale=4)
## integrate Cauchy Density from -Inf to -3
adaptIntegrate_inf_limPD(function(x) 1/pi * 1/(1+x^2), -Inf, -3)$int
stats::pcauchy(-3)
adaptIntegrate_inf_limPD(function(x, scale) 1/(pi*scale) * 1/(1+(x/scale)^2), -Inf, -3, scale=4)$int
stats::pcauchy(-3, scale=4)
```

 dkolm

Density for the Kolmogorov Distribution

Description

Density for the Kolmogorov Distribution

Usage

```
dkolm(x, nterms = 500, rep = "K3", K3cutpt = 2)
```

Arguments

x	domain value.
nterms	the number of terms in the limiting form's sum. That is, changing the infinity on the top of the summation to a big K.
rep	the representation. See article on webpage. Default is 'K3'.
K3cutpt	the cutpoint for rep='K3'. See article on webpage.

Value

the value of the density at specified x

Examples

```
## see https://swihart.github.io/mvdp/articles/deep\_dive\_kolm.html
dkolm(1)
```

dmvss

*Multivariate Subgaussian Stable Density***Description**

Computes the the density function of the multivariate subgaussian stable distribution for arbitrary alpha, shape matrices, and location vectors. See Nolan (2013).

Usage

```
dmvss(
  x,
  alpha = 1,
  Q = NULL,
  delta = rep(0, d),
  outermost.int = c("stats::integrate", "cubature::adaptIntegrate")[1],
  spherical = FALSE,
  subdivisions.si = 100L,
  rel.tol.si = .Machine$double.eps^0.25,
  abs.tol.si = rel.tol.si,
  stop.on.error.si = TRUE,
  tol.ai = 1e-05,
  fDim.ai = 1,
  maxEval.ai = 0,
  absError.ai = 0,
  doChecking.ai = FALSE,
  which.stable = c("libstable4u", "stabledist")[1]
)
```

Arguments

x	vector of quantiles.
alpha	default to 1 (Cauchy). Must be $0 < \alpha < 2$
Q	Shape matrix. See Nolan (2013).
delta	location vector
outermost.int	select which integration function to use for outermost integral. Default is "stats::integrate" and one can specify the following options with the .si suffix. For diagonal Q, one can also specify "cubature::adaptIntegrate" and use the .ai suffix options below (currently there is a bug for non-diagonal Q).
spherical	default is FALSE. If true, use the spherical transformation. Results will be identical to spherical = FALSE but may be faster.
subdivisions.si	the maximum number of subintervals. The suffix .si indicates a stats::integrate() option for the outermost semi-infinite integral in the product distribution formulation.

<code>rel.tol.si</code>	relative accuracy requested. The suffix <code>.si</code> indicates a <code>stats::integrate()</code> option for the outermost semi-infinite integral in the product distribution formulation.
<code>abs.tol.si</code>	absolute accuracy requested. The suffix <code>.si</code> indicates a <code>stats::integrate()</code> option for the outermost semi-infinite integral in the product distribution formulation.
<code>stop.on.error.si</code>	logical. If true (the default) an error stops the function. If false some errors will give a result with a warning in the message component. The suffix <code>.si</code> indicates a <code>stats::integrate()</code> option for the outermost semi-infinite integral in the product distribution formulation.
<code>tol.ai</code>	The maximum tolerance, default <code>1e-5</code> . The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>fDim.ai</code>	The dimension of the integrand, default <code>1</code> , bears no relation to the dimension of the hypercube. The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>maxEval.ai</code>	The maximum number of function evaluations needed, default <code>0</code> implying no limit. The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>absError.ai</code>	The maximum absolute error tolerated. The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>doChecking.ai</code>	A flag to be thorough checking inputs to C routines. A <code>FALSE</code> value results in approximately 9 percent speed gain in our experiments. Your mileage will of course vary. Default value is <code>FALSE</code> . The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>which.stable</code>	defaults to <code>"libstable4u"</code> , other option is <code>"stabledist"</code> . Indicates which package should provide the univariate stable distribution in this production distribution form of a univariate stable and multivariate normal.

Value

The object returned depends on what is selected for `outermost.int`. In the case of the default, `stats::integrate`, the value is a list of class `"integrate"` with components:

<code>value</code>	the final estimate of the integral.
<code>abs.error</code>	estimate of the modulus of the absolute error.
<code>subdivisions</code>	the number of subintervals produced in the subdivision process.
<code>message</code>	"OK" or a character string giving the error message.
<code>call</code>	the matched call.

Note: The reported `abs.error` is likely an under-estimate as `integrate` assumes the integrand was without error, which is not the case in this application.

References

Nolan, John P. "Multivariate elliptically contoured stable distributions: theory and estimation." Computational Statistics 28.5 (2013): 2067-2089.

Examples

```
## print("mvsubgaussPD (d=2, alpha=1.71):")
Q <- matrix(c(10,7.5,7.5,10),2)
mvpd::dmvss(x=c(0,1), alpha=1.71, Q=Q)

## more accuracy = longer runtime
mvpd::dmvss(x=c(0,1),alpha=1.71, Q=Q, abs.tol=1e-8)

Q <- matrix(c(10,7.5,7.5,7.5,10,7.5,7.5,7.5,10),3)
## print("mvsubgausPD (d=3, alpha=1.71):")
mvpd::dmvss(x=c(0,1,2), alpha=1.71, Q=Q)
mvpd::dmvss(x=c(0,1,2), alpha=1.71, Q=Q, spherical=TRUE)

## How `delta` works: same as centering
X <- c(1,1,1)
Q <- matrix(c(10,7.5,7.5,7.5,10,7.5,7.5,7.5,10),3)
D <- c(0.75, 0.65, -0.35)
mvpd::dmvss(X-D, alpha=1.71, Q=Q)
mvpd::dmvss(X , alpha=1.71, Q=Q, delta=D)
```

dmvss_mat

Multivariate Subgaussian Stable Density for matrix inputs

Description

Computes the the density function of the multivariate subgaussian stable distribution for arbitrary alpha, shape matrices, and location vectors. See Nolan (2013).

Usage

```
dmvss_mat(
  x,
  alpha = 1,
  Q = NULL,
  delta = rep(0, d),
  outermost.int = c("stats::integrate", "cubature::adaptIntegrate",
    "cubature::hcubature")[2],
  spherical = FALSE,
  subdivisions.si = 100L,
  rel.tol.si = .Machine$double.eps^0.25,
  abs.tol.si = rel.tol.si,
```

```

    stop.on.error.si = TRUE,
    tol.ai = 1e-05,
    fDim.ai = NULL,
    maxEval.ai = 0,
    absError.ai = 0,
    doChecking.ai = FALSE,
    which.stable = c("libstable4u", "stabledist")[1]
)

```

Arguments

<code>x</code>	nxd matrix of n variates of d-dimension
<code>alpha</code>	default to 1 (Cauchy). Must be $0 < \alpha < 2$
<code>Q</code>	Shape matrix. See Nolan (2013).
<code>delta</code>	location vector
<code>outermost.int</code>	select which integration function to use for outermost integral. Default is "stats::integrate" and one can specify the following options with the <code>.si</code> suffix. For diagonal Q, one can also specify "cubature::adaptIntegrate" and use the <code>.ai</code> suffix options below (currently there is a bug for non-diagonal Q).
<code>spherical</code>	default is FALSE. If true, use the spherical transformation. Results will be identical to <code>spherical = FALSE</code> but may be faster.
<code>subdivisions.si</code>	the maximum number of subintervals. The suffix <code>.si</code> indicates a <code>stats::integrate()</code> option for the outermost semi-infinite integral in the product distribution formulation.
<code>rel.tol.si</code>	relative accuracy requested. The suffix <code>.si</code> indicates a <code>stats::integrate()</code> option for the outermost semi-infinite integral in the product distribution formulation.
<code>abs.tol.si</code>	absolute accuracy requested. The suffix <code>.si</code> indicates a <code>stats::integrate()</code> option for the outermost semi-infinite integral in the product distribution formulation.
<code>stop.on.error.si</code>	logical. If true (the default) an error stops the function. If false some errors will give a result with a warning in the message component. The suffix <code>.si</code> indicates a <code>stats::integrate()</code> option for the outermost semi-infinite integral in the product distribution formulation.
<code>tol.ai</code>	The maximum tolerance, default 1e-5. The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>fDim.ai</code>	The dimension of the integrand, default 1, bears no relation to the dimension of the hypercube. The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>maxEval.ai</code>	The maximum number of function evaluations needed, default 0 implying no limit. The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.

<code>absError.ai</code>	The maximum absolute error tolerated The suffix <code>.ai</code> indicates a cubature: <code>:adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>doChecking.ai</code>	A flag to be thorough checking inputs to C routines. A <code>FALSE</code> value results in approximately 9 percent speed gain in our experiments. Your mileage will of course vary. Default value is <code>FALSE</code> . The suffix <code>.ai</code> indicates a cubature: <code>:adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>which.stable</code>	defaults to <code>"libstable4u"</code> , other option is <code>"stabledist"</code> . Indicates which package should provide the univariate stable distribution in this production distribution form of a univariate stable and multivariate normal.

Value

The object returned depends on what is selected for `outermost.int`. In the case of the default, `stats::integrate`, the value is a list of class "integrate" with components:

<code>value</code>	the final estimate of the integral.
<code>abs.error</code>	estimate of the modulus of the absolute error.
<code>subdivisions</code>	the number of subintervals produced in the subdivision process.
<code>message</code>	"OK" or a character string giving the error message.
<code>call</code>	the matched call.

Note: The reported `abs.error` is likely an under-estimate as `integrate` assumes the integrand was without error, which is not the case in this application.

References

Nolan, John P. "Multivariate elliptically contoured stable distributions: theory and estimation." *Computational Statistics* 28.5 (2013): 2067-2089.

Examples

```
## print("mvsubgaussPD (d=2, alpha=1.71):")
Q <- matrix(c(10,7.5,7.5,10),2)
mvpd::dmvss(x=c(0,1), alpha=1.71, Q=Q)

## more accuracy = longer runtime
mvpd::dmvss(x=c(0,1),alpha=1.71, Q=Q, abs.tol=1e-8)

Q <- matrix(c(10,7.5,7.5,7.5,10,7.5,7.5,7.5,10),3)
## print("mvsubgausPD (d=3, alpha=1.71):")
mvpd::dmvss(x=c(0,1,2), alpha=1.71, Q=Q)
mvpd::dmvss(x=c(0,1,2), alpha=1.71, Q=Q, spherical=TRUE)

## How `delta` works: same as centering
X <- c(1,1,1)
Q <- matrix(c(10,7.5,7.5,7.5,10,7.5,7.5,7.5,10),3)
D <- c(0.75, 0.65, -0.35)
```



```

mvpd::dmvss(X=D, alpha=1.71, Q=Q)
mvpd::dmvss(X , alpha=1.71, Q=Q, delta=D)

```

dmvt_mat

*Multivariate t-Distribution Density for matrix inputs***Description**

Computes the the density function of the multivariate subgaussian stable distribution for arbitrary degrees of freedom, shape matrices, and location vectors. See Swihart and Nolan (2022).

Usage

```

dmvt_mat(
  x,
  df = 1,
  Q = NULL,
  delta = rep(0, d),
  outermost.int = c("stats::integrate", "cubature::adaptIntegrate",
    "cubature::hcubature")[2],
  spherical = FALSE,
  subdivisions.si = 100L,
  rel.tol.si = .Machine$double.eps^0.25,
  abs.tol.si = rel.tol.si,
  stop.on.error.si = TRUE,
  tol.ai = 1e-05,
  fDim.ai = NULL,
  maxEval.ai = 0,
  absError.ai = 0,
  doChecking.ai = FALSE
)

```

Arguments

x	nxd matrix of n variates of d-dimension
df	default to 1 (Cauchy). This is df for t-dist, real number df>0. Can be non-integer.
Q	Shape matrix. See Nolan (2013).
delta	location vector
outermost.int	select which integration function to use for outermost integral. Default is "stats::integrate" and one can specify the following options with the .si suffix. For diagonal Q, one can also specify "cubature::adaptIntegrate" and use the .ai suffix options below (currently there is a bug for non-diagnoal Q).
spherical	default is FALSE. If true, use the spherical transformation. Results will be identical to spherical = FALSE but may be faster.

subdivisions.si	the maximum number of subintervals. The suffix .si indicates a stats::integrate() option for the outermost semi-infinite integral in the product distribution formulation.
rel.tol.si	relative accuracy requested. The suffix .si indicates a stats::integrate() option for the outermost semi-infinite integral in the product distribution formulation.
abs.tol.si	absolute accuracy requested. The suffix .si indicates a stats::integrate() option for the outermost semi-infinite integral in the product distribution formulation.
stop.on.error.si	logical. If true (the default) an error stops the function. If false some errors will give a result with a warning in the message component. The suffix .si indicates a stats::integrate() option for the outermost semi-infinite integral in the product distribution formulation.
tol.ai	The maximum tolerance, default 1e-5. The suffix .ai indicates a cubature::adaptIntegrate type option for the outermost semi-infinite integral in the product distribution formulation.
fDim.ai	The dimension of the integrand, default 1, bears no relation to the dimension of the hypercube. The suffix .ai indicates a cubature::adaptIntegrate type option for the outermost semi-infinite integral in the product distribution formulation.
maxEval.ai	The maximum number of function evaluations needed, default 0 implying no limit. The suffix .ai indicates a cubature::adaptIntegrate type option for the outermost semi-infinite integral in the product distribution formulation.
absError.ai	The maximum absolute error tolerated. The suffix .ai indicates a cubature::adaptIntegrate type option for the outermost semi-infinite integral in the product distribution formulation.
doChecking.ai	A flag to be thorough checking inputs to C routines. A FALSE value results in approximately 9 percent speed gain in our experiments. Your mileage will of course vary. Default value is FALSE. The suffix .ai indicates a cubature::adaptIntegrate type option for the outermost semi-infinite integral in the product distribution formulation.

Value

The object returned depends on what is selected for `outermost.int`. In the case of the default, `stats::integrate`, the value is a list of class "integrate" with components:

value	the final estimate of the integral.
abs.error	estimate of the modulus of the absolute error.
subdivisions	the number of subintervals produced in the subdivision process.
message	"OK" or a character string giving the error message.
call	the matched call.

Note: The reported `abs.error` is likely an under-estimate as `integrate` assumes the integrand was without error, which is not the case in this application.

References

Swihart & Nolan, "The R Journal: Multivariate Subgaussian Stable Distributions in R", The R Journal, 2022

Examples

```
x <- c(1.23, 4.56)
mu <- 1:2
Sigma <- matrix(c(4, 2, 2, 3), ncol=2)
df01 <- mvtnorm::dmvt(x, delta = mu, sigma = Sigma, df = 1, log=FALSE) # default log = TRUE!
df10 <- mvtnorm::dmvt(x, delta = mu, sigma = Sigma, df = 10, log=FALSE) # default log = TRUE!
df30 <- mvtnorm::dmvt(x, delta = mu, sigma = Sigma, df = 30, log=FALSE) # default log = TRUE!
df01
df10
df30

dmvt_mat(
  matrix(x,ncol=2),
  df = 1,
  Q = Sigma,
  delta=mu)$int

dmvt_mat(
  matrix(x,ncol=2),
  df = 10,
  Q = Sigma,
  delta=mu)$int

dmvt_mat(
  matrix(x,ncol=2),
  df = 30,
  Q = Sigma,
  delta=mu)$int

## Q: can we do non-integer degrees of freedom?
## A: yes for both mvpd::dmvt_mat and mvtnorm::dmvt

df1.5 <- mvtnorm::dmvt(x, delta = mu, sigma = Sigma, df = 1.5, log=FALSE) # default log = TRUE!
df1.5

dmvt_mat(
  matrix(x,ncol=2),
  df = 1.5,
  Q = Sigma,
  delta=mu)$int

## Q: can we do <1 degrees of freedom but >0?
## A: yes for both mvpd::dmvt_mat and mvtnorm::dmvt
```

```

df0.5 <- mvtnorm::dmvt(x, delta = mu, sigma = Sigma, df = 0.5, log=FALSE) # default log = TRUE!
df0.5

dmvt_mat(
  matrix(x,ncol=2),
  df = 0.5,
  Q = Sigma,
  delta=mu)$int

df0.0001 <- mvtnorm::dmvt(x, delta = mu, sigma = Sigma, df = 0.0001,
  log=FALSE) # default log = TRUE!
df0.0001

dmvt_mat(
  matrix(x,ncol=2),
  df = 0.0001,
  Q = Sigma,
  delta=mu)$int

## Q: can we do ==0 degrees of freedom?
## A: No for both mvpd::dmvt_mat and mvtnorm::dmvt

## this just becomes normal, as per the manual for mvtnorm::dmvt
df0.0 <- mvtnorm::dmvt(x, delta = mu, sigma = Sigma, df = 0, log=FALSE) # default log = TRUE!
df0.0

## Not run:
dmvt_mat(
  matrix(x,ncol=2),
  df = 0,
  Q = Sigma,
  delta=mu)$int

## End(Not run)

```

fit_mvss

Fit a Multivariate Subgaussian Distribution

Description

Estimates the parameters (namely, alpha, shape matrix Q, and location vector) of the multivariate subgaussian distribution for an input matrix X.

Usage

```
fit_mvss(x)
```

Arguments

`x` a matrix for which the parameters for a d-dimensional multivariate subgaussian distribution will be estimated. The number of columns will be d.

Details

Using the protocols outlined in Nolan (2013), this function uses `libstable4u`'s univariate fit functions for each component.

Value

A list with parameters from the column-wise univariate fits and the multivariate alpha and shape matrix estimates (the `univ_deltas` are the `mult_deltas`):

- `univ_alphas` - the alphas from the column-wise univariate fits
- `univ_betas` - the betas from the column-wise univariate fits
- `univ_gammas` - the gammas from the column-wise univariate fits
- `univ_deltas` - the deltas from the column-wise univariate fits
- `mult_alpha` - the mean(`univ_alphas`); equivalently the multivariate alpha estimate
- `mult_Q_raw` - the multivariate shape matrix estimate (before applying `nearPD()`)
- `mult_Q_posdef` - the nearest positive definite multivariate shape matrix estimate, `nearPD(mult_Q_raw)`

References

Nolan JP (2013), *Multivariate elliptically contoured stable distributions: theory and estimation*. Comput Stat (2013) 28:2067–2089 DOI 10.1007/s00180-013-0396-7

See Also

`Rfast::mvnorm.mle`, `alphastable::mfitstab.elliptical`

Examples

```
## create a 4x4 shape matrix symMat
S <- matrix(rnorm(4*4, mean=2, sd=4),4);
symMat <- as.matrix(Matrix::nearPD(0.5 * (S + t(S)))$mat)
symMat
## generate 10,000 r.v.'s from 4-dimensional mvss
X <- mvpd::rmvss(1e4, alpha=1.5, Q=symMat, delta=c(1,2,3,4))
## use fit_mvss to recover the parameters, compare to symMat
fmv <- mvpd::fit_mvss(X)
fmv
symMat
## then use the fitted parameters to calculate a probability:
mvpd::pmvss(lower=rep(0,4),
            upper=rep(5,4),
            alpha=fmv$mult_alpha,
            Q=fmv$mult_Q_posdef,
            delta=fmv$univ_deltas,
```

```
maxpts.pmvnorm = 25000*10)
```

mvpd

Multivariate Product Distributions

Description

The purpose of this package is to offer density, probability, and random variate generating (abbreviated as [d/p/r], respectively) functions for multivariate distributions that can be represented as a product distribution. Specifically, the package will primarily focus on the product of a multivariate normal distribution and a univariate random variable. These product distributions are called Scale Mixtures of Multivariate Normal Distributions, and for particular choices of the univariate random variable distribution the resultant product distribution may be a family of interest. For instance, the square-root of a positive stable random variable multiplied by a multivariate normal distribution is the multivariate subgaussian stable distribution. Product distribution theory is applied for implementing their computation.

Multivariate subgaussian stable distributions

`dmvss` – multivariate subgaussian stable distribution density

`pmvss` – multivariate subgaussian stable distribution probabilities

`rmvss` – multivariate subgaussian stable distribution random variates

`pmvss_mc` – Monte Carlo version of probabilities, using `rmvss`

`fit_mvss` – Fit a multivariate subgaussian stable distribution (e.g. estimate parameters given data)

Author(s)

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See Also

Useful links:

- <https://github.com/swihart/mvpd>
- <https://swihart.github.io/mvpd/>
- Report bugs at <https://github.com/swihart/mvpd/issues>

pmvlogis

*Multivariate Elliptically Contoured Logistic Distribution***Description**

Computes the probabilities for the multivariate elliptically contoured distribution for arbitrary limits, shape matrices, and location vectors.

Usage

```
pmvlogis(
  lower = rep(-Inf, d),
  upper = rep(Inf, d),
  nterms = 500,
  Q = NULL,
  delta = rep(0, d),
  maxpts.pmvnorm = 25000,
  abseps.pmvnorm = 0.001,
  outermost.int = c("stats::integrate", "cubature::adaptIntegrate")[1],
  subdivisions.si = 100L,
  rel.tol.si = .Machine$double.eps^0.25,
  abs.tol.si = rel.tol.si,
  stop.on.error.si = TRUE,
  tol.ai = 1e-05,
  fDim.ai = 1,
  maxEval.ai = 0,
  absError.ai = 0,
  doChecking.ai = FALSE
)
```

Arguments

lower	the vector of lower limits of length n.
upper	the vector of upper limits of length n.
nterms	the number of terms in the limiting form's sum. That is, changing the infinity on the top of the summation to a big K. This is an argument passed to dkolm().
Q	Shape matrix. See Nolan (2013).
delta	location vector.
maxpts.pmvnorm	Defaults to 25000. Passed to the $F_G = \text{pmvnorm}()$ in the integrand of the outermost integral.
abseps.pmvnorm	Defaults to 1e-3. Passed to the $F_G = \text{pmvnorm}()$ in the integrand of the outermost integral.
outermost.int	select which integration function to use for outermost integral. Default is "stats::integrate" and one can specify the following options with the .si suffix. For diagonal Q, one can also specify "cubature::adaptIntegrate" and use the .ai suffix options below (currently there is a bug for non-diagonal Q).

subdivisions.si	the maximum number of subintervals. The suffix .si indicates a stats::integrate() option for the outermost semi-infinite integral in the product distribution formulation.
rel.tol.si	relative accuracy requested. The suffix .si indicates a stats::integrate() option for the outermost semi-infinite integral in the product distribution formulation.
abs.tol.si	absolute accuracy requested. The suffix .si indicates a stats::integrate() option for the outermost semi-infinite integral in the product distribution formulation.
stop.on.error.si	logical. If true (the default) an error stops the function. If false some errors will give a result with a warning in the message component. The suffix .si indicates a stats::integrate() option for the outermost semi-infinite integral in the product distribution formulation.
tol.ai	The maximum tolerance, default 1e-5. The suffix .ai indicates a cubature::adaptIntegrate type option for the outermost semi-infinite integral in the product distribution formulation.
fDim.ai	The dimension of the integrand, default 1, bears no relation to the dimension of the hypercube. The suffix .ai indicates a cubature::adaptIntegrate type option for the outermost semi-infinite integral in the product distribution formulation.
maxEval.ai	The maximum number of function evaluations needed, default 0 implying no limit. The suffix .ai indicates a cubature::adaptIntegrate type option for the outermost semi-infinite integral in the product distribution formulation.
absError.ai	The maximum absolute error tolerated. The suffix .ai indicates a cubature::adaptIntegrate type option for the outermost semi-infinite integral in the product distribution formulation.
doChecking.ai	A flag to be thorough checking inputs to C routines. A FALSE value results in approximately 9 percent speed gain in our experiments. Your mileage will of course vary. Default value is FALSE. The suffix .ai indicates a cubature::adaptIntegrate type option for the outermost semi-infinite integral in the product distribution formulation.

Value

The object returned depends on what is selected for `outermost.int`. In the case of the default, `stats::integrate`, the value is a list of class "integrate" with components:

value	the final estimate of the integral.
abs.error	estimate of the modulus of the absolute error.
subdivisions	the number of subintervals produced in the subdivision process.
message	"OK" or a character string giving the error message.
call	the matched call.

Note: The reported `abs.error` is likely an under-estimate as `integrate` assumes the integrand was without error, which is not the case in this application.

References

Nolan JP (2013), *Multivariate elliptically contoured stable distributions: theory and estimation*.
 Comput Stat (2013) 28:2067–2089 DOI 10.1007/s00180-013-0396-7

Examples

```
## bivariate
U <- c(1,1)
L <- -U
Q <- matrix(c(10,7.5,7.5,10),2)
mvpd::pmvlogis(L, U, nterms=1000, Q=Q)

## trivariate
U <- c(1,1,1)
L <- -U
Q <- matrix(c(10,7.5,7.5,7.5,10,7.5,7.5,7.5,10),3)
mvpd::pmvlogis(L, U, nterms=1000, Q=Q)

## How `delta` works: same as centering
U <- c(1,1,1)
L <- -U
Q <- matrix(c(10,7.5,7.5,7.5,10,7.5,7.5,7.5,10),3)
D <- c(0.75, 0.65, -0.35)
mvpd::pmvlogis(L-D, U-D, nterms=100, Q=Q)
mvpd::pmvlogis(L, U, nterms=100, Q=Q, delta=D)

## recover univariate from trivariate
crit_val <- -1.3
Q <- matrix(c(10,7.5,7.5,7.5,20,7.5,7.5,7.5,30),3) / 10
Q
pmvlogis(c(-Inf,-Inf,-Inf),
         c( Inf, Inf, crit_val),
         Q=Q)
plogis(crit_val, scale=sqrt(Q[3,3]))

pmvlogis(c(-Inf, -Inf,-Inf),
         c( Inf, crit_val, Inf ),
         Q=Q)
plogis(crit_val, scale=sqrt(Q[2,2]))

pmvlogis(c( -Inf, -Inf,-Inf),
         c( crit_val, Inf, Inf ),
         Q=Q)
plogis(crit_val, scale=sqrt(Q[1,1]))
```

Description

Computes the probabilities for the multivariate subgaussian stable distribution for arbitrary limits, alpha, shape matrices, and location vectors. See Nolan (2013).

Usage

```
pmvss(
  lower = rep(-Inf, d),
  upper = rep(Inf, d),
  alpha = 1,
  Q = NULL,
  delta = rep(0, d),
  maxpts.pmvnorm = 25000,
  abseps.pmvnorm = 0.001,
  outermost.int = c("stats::integrate", "cubature::adaptIntegrate")[1],
  subdivisions.si = 100L,
  rel.tol.si = .Machine$double.eps^0.25,
  abs.tol.si = rel.tol.si,
  stop.on.error.si = TRUE,
  tol.ai = 1e-05,
  fDim.ai = 1,
  maxEval.ai = 0,
  absError.ai = 0,
  doChecking.ai = FALSE,
  which.stable = c("libstable4u", "stabledist")[1]
)
```

Arguments

lower	the vector of lower limits of length n.
upper	the vector of upper limits of length n.
alpha	default to 1 (Cauchy). Must be $0 < \alpha < 2$
Q	Shape matrix. See Nolan (2013).
delta	location vector.
maxpts.pmvnorm	Defaults to 25000. Passed to the $F_G = \text{pmvnorm}()$ in the integrand of the outermost integral.
abseps.pmvnorm	Defaults to $1e-3$. Passed to the $F_G = \text{pmvnorm}()$ in the integrand of the outermost integral.
outermost.int	select which integration function to use for outermost integral. Default is "stats::integrate" and one can specify the following options with the .si suffix. For diagonal Q, one can also specify "cubature::adaptIntegrate" and use the .ai suffix options below (currently there is a bug for non-diagonal Q).
subdivisions.si	the maximum number of subintervals. The suffix .si indicates a stats::integrate() option for the outermost semi-infinite integral in the product distribution formulation.

<code>rel.tol.si</code>	relative accuracy requested. The suffix <code>.si</code> indicates a <code>stats::integrate()</code> option for the outermost semi-infinite integral in the product distribution formulation.
<code>abs.tol.si</code>	absolute accuracy requested. The suffix <code>.si</code> indicates a <code>stats::integrate()</code> option for the outermost semi-infinite integral in the product distribution formulation.
<code>stop.on.error.si</code>	logical. If true (the default) an error stops the function. If false some errors will give a result with a warning in the message component. The suffix <code>.si</code> indicates a <code>stats::integrate()</code> option for the outermost semi-infinite integral in the product distribution formulation.
<code>tol.ai</code>	The maximum tolerance, default <code>1e-5</code> . The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>fDim.ai</code>	The dimension of the integrand, default <code>1</code> , bears no relation to the dimension of the hypercube. The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>maxEval.ai</code>	The maximum number of function evaluations needed, default <code>0</code> implying no limit. The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>absError.ai</code>	The maximum absolute error tolerated. The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>doChecking.ai</code>	A flag to be thorough checking inputs to C routines. A <code>FALSE</code> value results in approximately 9 percent speed gain in our experiments. Your mileage will of course vary. Default value is <code>FALSE</code> . The suffix <code>.ai</code> indicates a <code>cubature::adaptIntegrate</code> type option for the outermost semi-infinite integral in the product distribution formulation.
<code>which.stable</code>	defaults to <code>"libstable4u"</code> , other option is <code>"stabledist"</code> . Indicates which package should provide the univariate stable distribution in this production distribution form of a univariate stable and multivariate normal.

Value

The object returned depends on what is selected for `outermost.int`. In the case of the default, `stats::integrate`, the value is a list of class `"integrate"` with components:

<code>value</code>	the final estimate of the integral.
<code>abs.error</code>	estimate of the modulus of the absolute error.
<code>subdivisions</code>	the number of subintervals produced in the subdivision process.
<code>message</code>	"OK" or a character string giving the error message.
<code>call</code>	the matched call.

Note: The reported `abs.error` is likely an under-estimate as `integrate` assumes the integrand was without error, which is not the case in this application.

References

Nolan JP (2013), *Multivariate elliptically contoured stable distributions: theory and estimation*.
 Comput Stat (2013) 28:2067–2089 DOI 10.1007/s00180-013-0396-7

Examples

```
## bivariate
U <- c(1,1)
L <- -U
Q <- matrix(c(10,7.5,7.5,10),2)
mvpd::pmvss(L, U, alpha=1.71, Q=Q)

## trivariate
U <- c(1,1,1)
L <- -U
Q <- matrix(c(10,7.5,7.5,7.5,10,7.5,7.5,7.5,10),3)
mvpd::pmvss(L, U, alpha=1.71, Q=Q)

## How `delta` works: same as centering
U <- c(1,1,1)
L <- -U
Q <- matrix(c(10,7.5,7.5,7.5,10,7.5,7.5,7.5,10),3)
D <- c(0.75, 0.65, -0.35)
mvpd::pmvss(L-D, U-D, alpha=1.71, Q=Q)
mvpd::pmvss(L, U, alpha=1.71, Q=Q, delta=D)
```

pmvss_mc

Monte Carlo Multivariate Subgaussian Stable Distribution

Description

Computes probabilities of the multivariate subgaussian stable distribution for arbitrary limits, alpha, shape matrices, and location vectors via Monte Carlo (thus the suffix `_mc`).

Usage

```
pmvss_mc(
  lower = rep(-Inf, d),
  upper = rep(Inf, d),
  alpha = 1,
  Q = NULL,
  delta = rep(0, d),
  which.stable = c("libstable4u", "stabledist")[1],
  n = NULL
)
```

Arguments

lower	the vector of lower limits of length n.
upper	the vector of upper limits of length n.
alpha	default to 1 (Cauchy). Must be $0 < \alpha < 2$
Q	Shape matrix. See Nolan (2013).
delta	location vector.
which.stable	defaults to "libstable4u", other option is "stabledist". Indicates which package should provide the univariate stable distribution in this production distribution form of a univariate stable and multivariate normal.
n	number of random vectors to be drawn for Monte Carlo calculation.

Value

a number between 0 and 1, the estimated probability via Monte Carlo

References

Nolan JP (2013), *Multivariate elliptically contoured stable distributions: theory and estimation*.
 Comput Stat (2013) 28:2067–2089 DOI 10.1007/s00180-013-0396-7

Examples

```
## print("mvpd (d=2, alpha=1.71):")
U <- c(1,1)
L <- -U
Q <- matrix(c(10,7.5,7.5,10),2)
mvpd::pmvss_mc(L, U, alpha=1.71, Q=Q, n=1e3)
mvpd::pmvss (L, U, alpha=1.71, Q=Q)

## more accuracy = longer runtime
mvpd::pmvss_mc(L, U, alpha=1.71, Q=Q, n=1e4)

U <- c(1,1,1)
L <- -U
Q <- matrix(c(10,7.5,7.5,7.5,10,7.5,7.5,7.5,10),3)
## print("mvpd: (d=3, alpha=1.71):")
mvpd::pmvss_mc(L, U, alpha=1.71, Q=Q, n=1e3)
```

Description

Random Variates for the Kolmogorov Distribution

Usage

```
rkolm(n, nterms = 500)
```

Arguments

`n` the number of random variate to simulate

`nterms` the number of terms in the limiting sum. That is, turning infinity into a Big K on the top of the summation.

Value

`n` random variates

Examples

```
## see https://swihart.github.io/mvdp/articles/deep_dive_kolm.html
rkolm(10)
```

rmvlogis

Multivariate Logistic Random Variables

Description

Computes random vectors of the multivariate symmetric logistic distribution for arbitrary correlation matrices using the asymptotic Kolmogorov distribution – see references.

Usage

```
rmvlogis(n, Q = NULL, delta = rep(0, d), BIG = 500)
```

Arguments

`n` number of observations

`Q` semi-positive definite

`delta` location vector.

`BIG` the number of exponential to add for asymptotic Kolomogrov

References

Scale Mixtures of Normal Distributions Author(s): D. F. Andrews and C. L. Mallows Source: Journal of the Royal Statistical Society. Series B (Methodological), Vol. 36, No. 1 (1974), pp. 99-102
Published by: Wiley for the Royal Statistical Society Stable URL: <http://www.jstor.org/stable/2984774>

Examples

```

rmvlogis(10, Q=diag(5))

## Not run:
QMAT <- matrix(c(1,0,0,1),nrow=2)
draw_NNMD <- NonNorMvtDist::rmvlogis(2e3, parm1=rep(0,2), parm2=rep(1,2))
draw_mvpd <- mvpd::rmvlogis(2e3, Q=QMAT)

mean(draw_NNMD[,1] < -1 & draw_NNMD[,2] < 3)
mean(draw_mvpd[,1] < -1 & draw_mvpd[,2] < 3)

plogis(-1)
mean(draw_NNMD[,1] < -1)
mean(draw_mvpd[,1] < -1)

plogis(3)
mean(draw_NNMD[,2] < 3)
mean(draw_mvpd[,2] < 3)

rangex <- range(c(draw_mvpd[,1],draw_NNMD[,1]))
rangey <- range(c(draw_mvpd[,2],draw_NNMD[,2]))

par(mfrow=c(3,2), pty="s", mai=c(.5,.1,.1,.1))
plot(draw_NNMD, xlim=rangex, ylim=rangey); abline(h=0,v=0)
plot(draw_mvpd, xlim=rangex, ylim=rangey); abline(h=0,v=0)

hist(draw_NNMD[,1], breaks = 100, xlim=rangex, probability=TRUE, ylim=c(0,.40))
curve(dlogis(x), add=TRUE, col="blue",lwd=2)
hist(draw_mvpd[,1], breaks = 100, xlim=rangex, probability=TRUE, ylim=c(0,.40))
curve(dlogis(x), add=TRUE, col="blue",lwd=2)
hist(draw_NNMD[,2], breaks = 100, xlim=rangex, probability=TRUE, ylim=c(0,.40))
curve(dlogis(x), add=TRUE, col="blue",lwd=2)
hist(draw_mvpd[,2], breaks = 100, xlim=rangex, probability=TRUE, ylim=c(0,.40))
curve(dlogis(x), add=TRUE, col="blue",lwd=2)

## End(Not run)

```

 rmvss

Multivariate Subgaussian Stable Random Variates

Description

Computes random vectors of the multivariate subgaussian stable distribution for arbitrary alpha, shape matrices, and location vectors. See Nolan (2013).

Usage

```

rmvss(
  n,

```

```

alpha = 1,
Q = NULL,
delta = rep(0, d),
which.stable = c("libstable4u", "stabledist")[1]
)

```

Arguments

n	number of observations
alpha	default to 1 (Cauchy). Must be $0 < \alpha < 2$
Q	Shape matrix. See Nolan (2013).
delta	location vector.
which.stable	defaults to "libstable4u", other option is "stabledist". Indicates which package should provide the univariate stable distribution in this production distribution form of a univariate stable and multivariate normal.

Value

Returns the n by d matrix containing multivariate subgaussian stable random variates where $d = \text{nrow}(Q)$.

References

Nolan JP (2013), *Multivariate elliptically contoured stable distributions: theory and estimation*. Comput Stat (2013) 28:2067–2089 DOI 10.1007/s00180-013-0396-7

Examples

```

## generate 10 random variates of a bivariate mvss
rmvss(n=10, alpha=1.71, Q=matrix(c(10,7.5,7.5,10),2))

## generate 10 random variates of a trivariate mvss
Q <- matrix(c(10,7.5,7.5,7.5,10,7.5,7.5,7.5,10),3)
rmvss(n=10, alpha=1.71, Q=Q)

```


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